## Mathematics test

## Paper 2 Calculator allowed

## TIER

Please read this page, but do not open the booklet until your teacher tells you to start. Write your name and the name of your school in the spaces below. If you have been given a pupil number, write that also.

## First name

$\qquad$
Last name $\qquad$
School

## Pupil number



## Remember

- The test is 1 hour long.
- You may use a calculator in this test.
- You will need: pen, pencil, rubber, ruler, a pair of compasses, an angle measurer or protractor and a scientific or graphic calculator.
- $\quad$ Some formulae you might need are on page 2.
- This test starts with easier questions.
- Try to answer all the questions.
- Write all your answers and working on the test paper do not use any rough paper.
- Check your work carefully.
- Ask your teacher if you are not sure what to do.

|  | For marker's | Total marks |
| :--- | :--- | :--- |
| use only | Borderline check |  |
|  |  |  |

## Instructions

## Answers

This means write down your answer or show your working and write down your answer.

## Calculators

You may use a calculator to answer any question in this test.

## Formulae

You might need to use these formulae.

Trapezium


$$
\text { Area }=\frac{(a+b)}{2} \times h
$$

Prism


Volume $=$ area of cross-section $\times$ length

1. A drink from a machine costs 55p


The table shows the coins that were put into the machine one day.

| Coins | Number of coins |
| :---: | :---: |
| $50 p$ | 31 |
| $20 p$ | 22 |
| $10 p$ | 41 |
| $5 p$ | 59 |

How many cans of drink were sold that day?
Show your working.
2. You can work out the cost of an advert in a newspaper by using this formula:
$C=15 n+75$
C is the cost in pounds
$\boldsymbol{n}$ is the number of words in the advert
(a) An advert has 18 words.

Work out the cost of the advert.
Show your working.
(b) The cost of an advert is $\mathbf{f} \mathbf{6 1 5}$

How many words are in the advert?
Show your working.
3. (a) A coach travels $\mathbf{3 0 0}$ miles at an average speed of $\mathbf{4 0} \mathbf{~ m p h}$.

For how many hours does the coach travel?

hours
(b) An aeroplane flies $\mathbf{1 8 6 0}$ miles in $\mathbf{4}$ hours.

What is its average speed?

(c) A bus travels for $\mathbf{2} \frac{1}{2}$ hours at an average speed of $\mathbf{2 4} \mathbf{~ m p h}$. How far does the bus travel?
miles
4. A trundle wheel is used to measure distances.

Imran makes a trundle wheel, of diameter 50 cm .

(a) Calculate the circumference of Imran's trundle wheel.

Show your working.
cm
(b) Imran uses his trundle wheel to measure the length of the school car park.

His trundle wheel rotates 87 times.

What is the length of the car park, to the nearest metre?
m
1 mark
5. Draw lines to join any pairs of algebraic expressions that will always have the same value when $\boldsymbol{a}=\boldsymbol{b}=\boldsymbol{c}$


$$
3 c-2 b
$$

$2 c+b$
$a^{2}$
$a+c$
6. A teacher asked two different classes:
'What type of book is your favourite?'
(a) Results from class $A$ (total 20 pupils):

| Type of book | Frequency |
| :---: | :---: |
| Crime | 3 |
| Non-fiction | 13 |
| Fantasy | 4 |

Complete the pie chart to show this information.
Show your working and draw your angles accurately.

## Class A


(b) The pie chart below shows the results from all of class $\mathbf{B}$. Each pupil had only one vote.

## Class B



The sector for Non-fiction represents 11 pupils.
How many pupils are in class $B$ ?
Show your working.
pupils
7. (a) The label on yoghurt $A$ shows this information.

How many grams of protein does $\mathbf{1 0 0} \mathbf{g}$ of yoghurt provide?

Show your working.
(b) The label on yoghurt B shows different information.

A boy eats the same amount of yoghurt $A$ and yoghurt $B$.

Which yoghurt provides him with more carbohydrate?

Show your working.

## Yoghurt B $\mathbf{1 5 0 g}$

Each 150 g provides

| Energy | 339 kJ |
| :--- | ---: |
| Protein | 6.6 g |
| Carbohydrate | 13.1 g |
| Fat | 0.2 g |

8. (a) Calculate the length of the unknown side of this right-angled triangle. Show your working.

cm
(b) Calculate the length of the unknown side of the right-angled triangle below. Show your working.


Not drawn accurately
9. The goldcrest is Britain's smallest species of bird.

On winter days, a goldcrest must eat enough food to keep it warm at night. During the day, the mass of the bird increases.

The scatter diagram shows the mass of goldcrests at different times during winter days. It also shows the line of best fit.

(a) Estimate the mass of a goldcrest at 11:30 am.

9
(b) Estimate how many grams, on average, the mass of a goldcrest increases during one hour.


## g

(c) Which goldcrest represented on the scatter diagram is least likely to survive the night if it is cold?

Show your answer by circling the correct point on the scatter diagram, then explain why you chose that point.
10. (a) On the $\mathrm{cm}^{2}$ grid below, draw a right-angled triangle with an area of $12 \mathbf{c m}^{2}$ Use line $A B$ as one side of the triangle.

(b) Now draw an isosceles triangle with an area of $12 \mathbf{c m}^{2}$ Use line $A B$ as one side of the triangle.

(c) Use Pythagoras' theorem to prove that $\mathbf{A C}$ is the same length as $\mathbf{A B}$


Show your working.
(d) Calculate the size of angle ABC Show your working.
11. A gardener wants to plant a tree.

She wants it to be more than $\mathbf{8 m}$ away from the vegetable plot.
She wants it to be more than $\mathbf{1 8} \mathbf{m}$ away from the greenhouse.

The plan below shows part of the garden.
The scale is $\mathbf{1 \mathbf { c m }}$ to $\mathbf{4 m}$.

Show accurately on the plan the region of the garden where she can plant the tree.

Label this region $\mathbf{R}$.

12. The table shows the average weekly earnings for men and women in 1956 and 1998.

|  | 1956 | 1998 |
| :---: | :---: | :---: |
| Men | $£ 11.89$ | $£ 420.30$ |
| Women | $£ 6.16$ | $£ 303.70$ |

(a) For 1956, calculate the average weekly earnings for women as a percentage of the average weekly earnings for men.

Show your working and give your answer to 1 decimal place.
\%
(b) For 1998, show that the average weekly earnings for women were a greater proportion of the average weekly earnings for men than they were in 1956.
13. A shop had a sale. All prices were reduced by $15 \%$

A pair of shoes cost $£ \mathbf{3 8 . 2 5}$ in the sale.
What price were the shoes before the sale?
Show your working.
14. The diagram shows a sketch of the curve $y=16-x^{2}$

(a) What are the coordinates of points $A, B$ and $C$ ?
$\geqslant$
A 1
B 1
C 1

The curve $y=16-x^{2}$ is reflected in the line $y=12$

(b) $B_{1}$ is the reflection of $B$

What are the coordinates of $B_{1}$ ?

(c) What is the equation of the new curve?
15. The diagram shows parts of two circles, sector $A$ and sector $B$

(a) Which sector has the bigger area?

Show working to explain your answer.
(b) The perimeter of a sector is made from two straight lines and an arc.

Which sector has the bigger perimeter?
Show working to explain your answer.
(c) A semi-circle, of radius 4 cm , has the same area as a complete circle of radius $r \mathrm{~cm}$.


Not drawn accurately

What is the radius of the complete circle?
Show your working.
16. Each year a school has a concert of readings and songs.

In 1999 the concert had 3 readings and 9 songs. It lasted 120 minutes.

In 2000 the concert had 5 readings and 5 songs. It lasted 90 minutes.

In 2001 the school plans to have 5 readings and 7 songs.

Use simultaneous equations to estimate how long the concert will last.
Call the time estimated for a reading $x$ minutes, and the time estimated for a song $y$ minutes.

You must show your working.

END OF TEST

