Mathematics test

Paper 2
Calculator allowed

Please read this page, but do not open your booklet until your teacher tells you to start. Write your name and the name of your school in the spaces below.

First name ________________________________
Last name ________________________________
School _________________________________

Remember

■ The test is 1 hour long.
■ You may use a calculator for any question in this test.
■ You will need: pen, pencil, rubber, ruler, a pair of compasses and a scientific or graphic calculator.
■ Some formulae you might need are on page 2.
■ This test starts with easier questions.
■ Try to answer all the questions.
■ Write all your answers and working on the test paper – do not use any rough paper. Marks may be awarded for working.
■ Check your work carefully.
■ Ask your teacher if you are not sure what to do.

For marker’s use only

<table>
<thead>
<tr>
<th>Total marks</th>
</tr>
</thead>
<tbody>
<tr>
<td>____________</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Borderline check</th>
</tr>
</thead>
<tbody>
<tr>
<td>________________</td>
</tr>
</tbody>
</table>
Instructions

Answers
This means write down your answer or show your working and write down your answer.

Calculators
You may use a calculator to answer any question in this test.

Formulae
You might need to use these formulae

### Trapezium

Area = \( \frac{1}{2}(a + b)h \)

### Prism

Volume = area of cross-section \( \times \) length
1. I buy **12 packets** of cat food in a box.

   The table shows the different varieties in the box.

<table>
<thead>
<tr>
<th>Variety</th>
<th>Number of packets</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cod</td>
<td>3</td>
</tr>
<tr>
<td>Salmon</td>
<td>3</td>
</tr>
<tr>
<td>Trout</td>
<td>3</td>
</tr>
<tr>
<td>Tuna</td>
<td>3</td>
</tr>
</tbody>
</table>

   (a) I am going to take out a packet at random from the box.
   
   What is the **probability** that it will be **cod**?

   - 1 mark

   (b) My cat eats **all** the packets of **cod**.
   
   I am going to take out a packet at random from the ones left in the box.
   
   What is the **probability** that it will be **salmon**?

   - 1 mark

   (c) A different type of cat food has **10 packets** in a box.
   
   The probability that the variety is chicken is **0.7**
   
   What is the probability that the variety is **not** chicken?

   - 1 mark
2. Wine gums are sweets that are made in different colours.

Pupils tested whether people can taste the difference between black wine gums and other wine gums.

The percentage bar charts show three pupils’ results.

Key:
- Cannot taste the difference
- Can taste the difference

Ravi asked 50 people
Sita asked 100 people
Tina asked 200 people
(a) Complete the table.

<table>
<thead>
<tr>
<th></th>
<th>Number of people who were tested</th>
<th>Number of people who can taste the difference</th>
<th>Number of people who cannot taste the difference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ravi</td>
<td>50</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Sita</td>
<td>100</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Tina</td>
<td>200</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

(b) Explain why Tina's results are likely to be more reliable than Ravi's or Sita's.

3. Look at the three expressions below.

\[ 8 + k \quad 3k \quad k^2 \]

When \( k = 10 \), what is the value of each expression?

\[ 8 + k = \quad 3k = \quad k^2 = \]

2 marks
4. Some statements in the table are true. Some are false. Beside each statement, write **true** or **false**. For **true** statements you must **draw an example**. The first one is done for you.

<table>
<thead>
<tr>
<th>Statement</th>
<th>Write <strong>true</strong> or <strong>false</strong>. If true, draw an example.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Some triangles have one right angle and two acute angles.</td>
<td><strong>true</strong></td>
</tr>
<tr>
<td>Some triangles have three right angles.</td>
<td></td>
</tr>
<tr>
<td>Some triangles have three acute angles.</td>
<td></td>
</tr>
<tr>
<td>Some triangles have one obtuse angle and two acute angles.</td>
<td></td>
</tr>
<tr>
<td>Some triangles have two obtuse angles and one acute angle.</td>
<td></td>
</tr>
</tbody>
</table>
5. A shop sells toilet rolls. You can buy them in packs of 9 or packs of 6

Which pack gives you better value for money?

You must show your working.
6. Three different types of woodpecker live in Britain.

The pictogram shows information about the numbers of each type.

<table>
<thead>
<tr>
<th>Type</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Type A</td>
<td>great spotted woodpecker</td>
</tr>
<tr>
<td>Type B</td>
<td>lesser spotted woodpecker</td>
</tr>
<tr>
<td>Type C</td>
<td>green woodpecker</td>
</tr>
</tbody>
</table>

Key: 🦜 represents 10,000 woodpeckers

(a) Complete the table below to show the percentages of each type of woodpecker.

<table>
<thead>
<tr>
<th>Type A</th>
<th>Type B</th>
<th>Type C</th>
</tr>
</thead>
<tbody>
<tr>
<td>______</td>
<td>______</td>
<td>______</td>
</tr>
</tbody>
</table>

1 mark
(b) The ratio of type A : type B woodpeckers is $6 : 1$

What is the ratio of type B : type C woodpeckers?

____ : ____  

1 mark

7. Write the missing numbers in the boxes.

120mm is the same as __ cm  

1 mark

120cm is the same as __ m  

1 mark

120m is the same as __ km  

1 mark
8. Look at the diagram, made from four straight lines.

The lines marked with arrows are parallel.

\[ a = \quad ^\circ \quad b = \quad ^\circ \]

\[ c = \quad ^\circ \quad d = \quad ^\circ \]

Work out the sizes of the angles marked with letters.
9. Look at this equation.

\[ 3a + 20 = 4a + k \]

(a) If \( a = 15 \), find the value of \( k \)

\[ k = \underline{\phantom{0}} \]

(b) If \( a = -15 \), find the value of \( k \)

\[ k = \underline{\phantom{0}} \]
10. Each shape below is made from **five cubes** that are joined together.

Complete the missing diagrams below.

<table>
<thead>
<tr>
<th>Shape drawn on an isometric grid</th>
<th>View from above of the shape drawn on a square grid</th>
</tr>
</thead>
<tbody>
<tr>
<td><img src="image1.png" alt="Shape 1" /></td>
<td><img src="image2.png" alt="View 1" /></td>
</tr>
<tr>
<td><img src="image3.png" alt="Shape 2" /></td>
<td><img src="image4.png" alt="View 2" /></td>
</tr>
<tr>
<td><img src="image5.png" alt="Shape 3" /></td>
<td><img src="image6.png" alt="View 3" /></td>
</tr>
</tbody>
</table>
11. Look at these pairs of number sequences.

The second sequence is formed from the first sequence by adding a number or multiplying by a number.

Work out the missing \( n \)th terms.

(a) \( 5, 9, 13, 17, \ldots \) \( n \)th term is \( 4n + 1 \)

(b) \( 12, 18, 24, 30, \ldots \) \( n \)th term is \( 6n + 6 \)

(c) \( 2, 7, 12, 17, \ldots \) \( n \)th term is \( 5n - 3 \)
12. Look at the square grids.

Each diagram shows an enlargement of scale factor 2

The **centre** of this enlargement is marked with a cross.

Where is the centre of enlargement in these diagrams?

Mark each one with a cross.
13. Multiply out these expressions.
Write your answers as simply as possible.

\[ 5(x + 2) + 3(7 + x) \]

\[ (x + 2)(x + 5) \]
14. Kate asked people if they read a daily newspaper. Then she wrote this table to show her results.

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>No</strong></td>
<td>80 people = 40%</td>
</tr>
<tr>
<td><strong>Yes</strong></td>
<td>126 people = 60%</td>
</tr>
</tbody>
</table>

The values in the table **cannot** all be correct.

(a) The error could be in the number of people. Complete each table to show what the correct numbers could be.

<p>| | |</p>
<table>
<thead>
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</tr>
<tr>
<td><strong>Yes</strong></td>
<td>126 people = 60%</td>
</tr>
</tbody>
</table>
(b) The error could be in the percentages.

Complete the table with the correct percentages.

<table>
<thead>
<tr>
<th></th>
<th>80 people = _____ %</th>
</tr>
</thead>
<tbody>
<tr>
<td>No</td>
<td></td>
</tr>
<tr>
<td>Yes</td>
<td>126 people = _____ %</td>
</tr>
</tbody>
</table>
15. The graph shows information about the diameters and heights of a sample of three types of tomato.

The dotted lines on the graph can be used to decide which type of tomato each point is likely to represent.

(a) The diameter of a tomato of **type C** is **11 cm**.

What would you expect its height to be?
(b) The diameter of a different tomato is 3.2 cm. Its height is 5.8 cm. Which of the three types of tomato is it most likely to be? 

A  B  C

Explain your answer.

(c) Which type of tomato is most nearly **spherical** in shape? 

A  B  C

Explain your answer.

(d) You can find the approximate volume of a tomato by using this formula:

\[ V = \frac{1}{6} \pi d^2 h \]

V is the volume, 
\( d \) is the diameter, 
\( h \) is the height.

The diameter and the height of a tomato are both **3.5 cm**. What is the approximate volume of this tomato?

\[ \] cm³

1 mark

1 mark

2 marks
16. In a wildlife park in Africa, wardens want to know the position of an elephant in a certain area.

They place one microphone at each corner of a 4 km by 4 km square. Each microphone has a range of $3\frac{1}{2}$ km.

The elephant is out of range of microphones A and B.

Where in the square could the elephant be?

Show the region accurately on the diagram, and label the region R.
Here are the rules for an algebra grid.

This value is the **sum** of the values in the middle row.

This value is the **product** of the values in the middle row.

Use these rules to complete the algebra grids below.
Write your expressions as simply as possible.
18. This shape is made of four congruent kites meeting at a point.

Calculate the size of angle $k$

$$k = \phantom{00}^\circ$$

2 marks
19. Look at the diagram of a cuboid.

The volume of the cuboid is \(100\text{cm}^3\)

What could the values of \(x\) and \(y\) be?
Give two possible pairs of values.

\[
x = \underline{\hphantom{00}}, \quad y = \underline{\hphantom{00}}\quad \text{1 mark}
\]

\[
x = \underline{\hphantom{00}}, \quad y = \underline{\hphantom{00}}\quad \text{1 mark}
\]
20. A pupil wants to investigate a report that Belgian one euro coins are biased in favour of heads.

Here is her plan for the investigation.

I will spin **20** Belgian one euro coins to give one set of results.

I will do this **10 times** to give a total of **200 results** to work out an estimated probability of spinning a head.

If this probability is **greater than 56%** my conclusion will be that Belgian one euro coins are biased in favour of heads.

The table shows the 10 sets of results.

| Number of each set of **20** coins that showed heads |
|---|---|---|---|---|---|---|
| 10 | 13 | 11 | 11 | 12 | 12 | 11 |
| 9  | 10 | 11 |    |    |    |    |

Using the pupil’s plan, what should her conclusion be?

You **must** show your working.
21. The diagram shows a shaded rectangle. It is divided into four smaller rectangles, labelled A, B, C and D.

The ratio of area C to area B is 1 : 2

Calculate area A.
22. Field voles are small animals that do not live for very long.

A scientist recorded data on 1000 of these voles that were born on the same day.

The graph shows how many voles were still alive after a number of weeks.

Use the graph to answer this question.

Estimate the probability that a field vole will live to be at least 20 weeks old.